Joint Resource Allocation for Software Defined Networking, Caching and Computing

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Abstract—Recently, there are significant advances in the areas of networking, caching and computing. Nevertheless, these three important areas have traditionally been addressed separately in the existing research. In this paper, we present a novel framework that integrates networking, caching and computing in a systematic way and enables dynamic orchestration of these three resources to improve the end-to-end system performance and meet the requirements of different applications. Then, we consider the bandwidth, caching and computing resource allocation issue and formulate it as a joint caching/computing strategy and servers selection problem to minimize the combination cost of network usage and energy consumption in the framework. To minimize the combination cost of network usage and energy consumption in the framework, we formulate it as a joint caching/computing strategy and servers selection problem. In addition, we solve the joint caching/computing strategy and servers selection problem using an exhaustive-search algorithm. Simulation results show that our proposed framework significantly outperforms the traditional network without in-network caching/computing in terms of network usage and energy consumption.

Index Terms—Networking, caching, computing, resource allocation, energy efficient.

I. INTRODUCTION

Recently, there are significant advances in the areas of networking, caching and computing, which can have profound impacts on our society though the developments of smart cities, smart transportation, smart homes, etc. Software-defined networking (SDN) has been considered as one of the most promising technologies on realization of programmable networking, and has been deployed well in existing IP networks, such as Internet service providers and data center networks [1], [2]. By separating the control plane (decision functions) from the data plane (forwarding functions) in networks, SDN enables the development of new routing and forwarding approaches without the need to replace hardware components in the core network, simplifying network management and facilitating network evolution [3]–[7].

In the area of caching, information-centric networking (ICN), which has been extensively studied in recent years [8], [9], enables in-network caching to reduce the duplicate content transmission in networks [10]. By focusing on the data’s names instead of their locations, ICN provides native support for secure communication, scalable and efficient content distribution, and the enhanced capability for mobility [11]–[15]. In the area of computing, cloud computing paradigm has been widely adopted to utilize the computing resources in remote provider’s servers via the Internet, providing enterprises and end users with a range of application services and freeing them from the specification of many details [16]–[22]. Nevertheless, it is not feasible or economical to satisfy current applications requirements of mobility support, location awareness, low latency and big data analytics as the distance between the cloud and the edge device is usually large. To address these issues, fog computing has been proposed to extend cloud computing and services close to end devices [23], [24]. A similar technique, called mobile edge computing, is being standardized to allocate computing resources in wireless access networks [25].

How to manage, control and optimize network, cache and compute (the three important underlying resources) can have great impacts on the performance of system and applications. Currently, in the works of SDN and ICN, these three resources are traditionally addressed separately, which could result in suboptimal performance. We present a novel framework called SD-NCC (Software Defined Networking, Caching and Computing) that integrates networking, caching and computing in a systematic way to meet the requirements of different applications and improve the end-to-end system performance. As Fig. 1 shows, the SD-NCC framework can be divided in three planes of functionality: data, control, and management planes (similar to SDN). Different from SDN, the added in-network caching and computing in the data plane become inherent fundamental capabilities in SD-NCC. Thus, besides the software defined networking, SD-NCC enables the software defined caching and computing. Additionally, each data packet carries a name and a signature (similar to ICN), thus enabling information centric paradigm.

Based on the SD-NCC framework, we present a comprehensive system model and formulate a joint caching/computing strategy and servers selection problem as a mixed-integer nonlinear programming (MINLP) problem to minimize the combination cost of network usage and energy consumption. Specifically, we formulate the caching/computing capacity allocation problem and derive the optimal deployment numbers
of service copies. In addition, we develop an exhaustive-search algorithm to find the optimal caching/computing strategy and servers selection strategy. Simulation results show that compared with traditional network, our proposed SD-NCC framework significantly reduces the traffic traversing the network and has performance advantage on energy consumption cost. We also show the impact of service popularity on optimal deployment number of service copies.

The rest of the article is organized as follows. Section II presents a system model for this framework. Section III formulates the joint bandwidth, caching and computing resource allocation problem and work out a near-optimal caching/computing strategy and servers selection solution. Simulation results are discussed in Section IV. Finally, we conclude this paper in Section V.

II. SYSTEM MODEL

In this section, we present the system model for the SD-NCC framework.

A. Network Model

Consider a network represented by graph $G = \{V, E\}$, where $V$ denotes the set of nodes and $E$ denotes the set of directed physical links. A node can be a router, a user, or a server. We introduce the following notation:

- $S = \{S_A, S_B\}$, the set of in-network server nodes; $S_A \subset V$, the set of caching nodes; $S_B \subset V$, the set of computing nodes.
- $\mathcal{O}$, a single virtual origin node which is always able to serve the request services.
- $U$, the set of users who issue service requests, $U \subset V$.
- $K = \{K_A, K_B\}$, the set of service elements; $K_A$, the set of content elements; $K_B$, the set of computation services.
- $\lambda_k$, the number of content $k$’s requests for duration $t$; $\alpha_k$, the size of content $k$.
- $\lambda_k^A$, $\alpha_k^A$, the number of content $k$’s requests for duration $t$; $\alpha_k^B$, the size of content $k$.
- $\lambda_k^B$, $\alpha_k^B$, the number of computation $k$’s data communications, $k \in K_B$; $c_k$, the amount of computation $k$’s workload (which can be measured by the number of clock cycles or execution time).

B. Caching/Computing Model

Let $c_i^A$, $c_i^B$ denote the caching capacity and computing capacity of server node $i$. We assume the finite capacity of in-network server nodes and the infinite capacity of original server. We use $H : \{h_i^k\}$ to denote the caching/computing strategy matrix, where $h_i^k = 1$ if server $i$ is able to provide the requested service $k$ and $h_i^k = 0$ if it is not. Specifically, $h_i^k = 1$.

Thus, the caching/computing capacity constraints are as follows:

$$\sum_k h_i^k c_i^A \leq c_i^A, \forall i \in S_A$$ (1)

and

$$\sum_k h_i^k c_i^B \leq c_i^B, \forall i \in S_B$$ (2)

Fig. 1. Software-defined networking, caching, and computing in (a) planes and (b) system design architecture.
C. Servers Selection Model

Let $P: \{p_{k,u}^i\}$ denote the servers selection matrix, where $p_{k,u}^i \in [0, 1]$ denotes the proportion of the service request $k$ from user $u$ served by server $i$. Node $u$ can be viewed as an edge router that aggregates the traffic of many endhosts, which may be served by different servers. Let $X: \{x_{k,i,u}^v\}$ denote the traffic allocation matrix, where $x_{k,i,u}^v$ denotes the traffic of service $k$ from user $u$ to server $i$ for duration $t$. Combining with the caching/computing strategy, we have
\[
x_{k,i,u}^v = m_{u}^k p_{i,u}^k h_{1}^k, \forall i \in S \cup \{o\}
\]
and
\[
\sum_i p_{i,u}^k h_{1}^k = 1
\]

D. Routing Model

Let $R: \{r_{i,u}^v\}$ be the routing matrix, where $r_{i,u}^v \in [0, 1]$ denotes the proportion of traffic from user $u$ to server $i$ that traverses link $l$. $r_{i,u}^v$ equals 1 if the link $l$ is on the path from server $i$ to user $u$ and 0 otherwise.

Then the routing selection strategy is given by
\[
\sum_{l \in I_n(v)} r_{i,u}^v - \sum_{l \in O_{out}(v)} r_{i,u}^v = I_{v = i}, \forall i \in S \cup \{o\}, v \in V \setminus U
\]
where $I_{v = i}$ is an indicator function which equals 1 if $v = i$ and 0 otherwise, $I_n(v)$ denotes the set of incoming links to node $v$, and $O_{out}(v)$ denotes the set of outgoing links from node $v$.

The capacity of a link $l$ is $c_l$. Thus, the total traffic traversing link $l$ denoted by $x_l$ is given by
\[
x_l = \sum_{k,i,u} x_{k,i,u}^v r_{i,u}^v \leq c_l, \forall i \in S \cup \{o\}
\]

E. Energy Model

The escalation of energy consumption in networks directly results in the increase of greenhouse gas emission, which has been recognized as a major threat for environmental protection and sustainable development [26]-[31]. The energy is mainly consumed by content caching, data computing and traffic transmission in SD-NCC framework. We discuss these three energy models as follows.

1) Caching Energy: $E_{ca}^A$, we use an energy-proportional model, similar to [32]. If $n_{k_1}$ copies of the content $k_1$ are cached for duration $t$, the energy consumed by caching $n_k o_k^A$ bits is given by
\[
E_{ca,k_1}^A = n_k o_k^A p_{ca}^A t
\]
where $p_{ca}^A$ is the power efficiency of caching. The value of $p_{ca}^A$ strongly depends on the caching hardware technology.

2) Computing Energy: We assume that computation applications are executed within the virtual machines (VMs) which are deployed on the computing nodes and the amount of incoming computation $k_2$’s workloads from all users is $\lambda_{k_2}^B$ for duration $t$. The energy consumption of the computing nodes consists of two parts, including a dynamic energy consumption part $E_{active}^B$ when the VMs are active (processing computing service requests) and a static energy consumption part $E_{static}^B$ when the VMs are idle.

Thus, the dynamic energy consumption on processing the workloads is
\[
E_{active}^B = \lambda_{k_2}^B c_{k_2} p_{active}^B
\]
and the static energy consumption for $m_{k_2}$ copies of computation $k_2$’s dedicated VM is
\[
E_{static}^B = m_{k_2} p_{static}^B t
\]
where $p_{active}^B, p_{static}^B$ are the average power efficiency of VMs in active and static states, respectively.

Note that the dynamic energy consumption is independent of the VMs’ copies.

3) Transmission Energy: The transmission energy $E_{tr}$ consumption mainly consists of the energy consumption at routers and energy consumption along the links.

The transmission energy of content $E_{tr}^A$ and computation $E_{tr}^B$ for duration $t$ are given by
\[
E_{tr,k_1}^A = \lambda_{k_1}^A o_{k_1}^A \left[ p_{tr,link} \cdot d_{k_1}^A + p_{tr,node} \cdot (d_{k_1}^A + 1) \right]
\]
\[
E_{tr,k_2}^B = \lambda_{k_2}^B o_{k_2}^B \left[ p_{tr,link} \cdot d_{k_2}^B + p_{tr,node} \cdot (d_{k_2}^B + 1) \right]
\]
where $p_{tr,link}$ and $p_{tr,node}$ are the energy efficiency parameters of the link and node respectively, $d_{k_1}^A$ and $d_{k_2}^B$ represent the average hop distance to the content server nodes for content $k_1$’s request and the computation server nodes for computation $k_2$’s request, respectively.

III. CACHING/COMPUTING/BANDWIDTH RESOURCE ALLOCATION

In this subsection, we consider the joint caching, computing and bandwidth resource allocation problem and formulate it as a joint caching/computing strategy and servers selection problem (CCS-SS) which we show is a mixed integer nonlinear programming (MINLP) problem. By relaxing the whole caching, computing, link constraints, we focus on the caching/computing capacity allocation for each service element and formulate it as a nonlinear programming (NLP) problem. We derive the optimal caching/computing capacity allocation (i.e., the copies number for each service element) and then propose an exhaustive-search algorithm to find the optimal caching/computing strategy and servers selection.

A. Problem Formulation

1) Objective Function: Based on the known topology, traffic matrix, routing matrix and the energy parameters of network equipments, we introduce the following quantities:

- $d_{i,u}$, the hop distance between server node $i$ and user $u$;
- $D_{i,u}$, the end-to-end latency between server node $i$ and user $u$;
- $a_{i,u} = p_{tr,link} d_{i,u} + p_{tr,node} (d_{i,u} + 1)$, the energy for transporting per bit from server node $i$ to user $u$;
- $f_{u,cr} = \sum_{k \in K} \sum_{i \in S} \sum_{u \in U} a_{i,u} m_{k,u} p_{i,u}^k h_{1}^k$, the transmission energy for duration $t$;
\[ f_{ca}(h_k^t) = \sum_{k \in K_A} \sum_{u \in S_A} h_k^t \rho_{k,u}^t \rho_{ca}^t \], the caching energy for duration \( t \);

\[ f_{com} = \sum_{k \in K_B} \sum_{u \in S_B} h_k^B \rho_{k,u}^B t + \sum_{k_2 \in K_B} \lambda_{k_2}^B \rho_{k_2}^B \], the energy consumption on computing nodes for duration \( t \);

\[ f_{tr} = \sum_{k \in K} \sum_{u \in S_k(\{o\}) \cup \{u\}} D_{i,u} m_i^u \rho_{k,i,u}^t h_k^t \], the network traffic for duration \( t \).

We select a combining objective which balances the energy costs and the network usage costs for duration \( t \). The cost function is given by

\[
f = f_{ca}(h_k^t) + f_{com}(h_k^t) + f_{tr}(\rho_{k,i,u}^t, h_k^t) + \gamma f_{tr}(\rho_{k,i,u}^t, h_k^t)
\]

where \( \gamma \) is the weight between the two costs. The first three parts constitute the energy consumption for duration \( t \) and the last one is network traffic which denotes the network usage in this paper.

2) Formulation: In the following, we formulate the CCS-SS problem to minimize the combination cost function. The optimization problem is shown as follows:

\[
\begin{align*}
\min \, f(h_k^t, \rho_{k,i,u}^t) \\
s.t. \quad C1 : \sum_i \rho_{k,i,u}^t h_k^t = 1 \\
C2 : \sum_k h_k^t \rho_{k,i,u}^t \leq c_i^t, \forall i \in S_A \\
C3 : \sum_k h_k^t \rho_{k,i,u}^t \leq c_i^t, \forall i \in S_B \\
C4 : x_i = \sum_{k,i,u} m_i^u \rho_{k,i,u}^t h_k^t + c_i, \forall i \in S \cup \{o\} \\
C5 : h_k^t \in \{0, 1\}, \rho_{k,i,u}^t \in [0, 1]
\end{align*}
\]

Constraints (1) specifies that user \( u \)'s demand rate for service \( k \) can be served by several servers simultaneously depending on caching/computing strategy and servers selection strategy. Constraints (2) and (3) specify the caching/computing resource capacity limits on in-network server nodes. Data rates are subject to link capacity constraint (4).

Problem (13) is difficult to solve based on the following observations:

- Both the objective function and feasible set of (13) are not convex due to the binary variables \( h_k^t \) and the product relationship between \( h_k^t \) and \( \rho_{k,i,u}^t \).

- The size of the problem is very large. For instance, if there are \( F \) service elements and \( N \) network nodes, the number of variables \( h_k^t \) is \( N^F \). In future networks, the number of the service elements and network nodes will rise significantly.

As is well known, a MINLP problem is expected to be NP-hard [33], and a variety of algorithms are capable of solving instances with hundreds or even thousands of variables. However, it is very challenging to find the global optimum resource allocation in our problem, since the number of variables and the constraints grow exponentially. How to efficiently solve it is left for future research. Instead, in the next subsection, we propose an NLP formulation from a different view which can be solved analytically.

**B. Caching/Computing Capacity Allocation**

In this section, we focus on the optimal caching/computing capacity allocated for each service \( k \), but not the optimal cache location. We denote \( n_{k_1} \) as the number of content \( k_1 \)'s copies and \( m_{k_2} \) as the number of computation \( k_2 \)'s dedicated VM copies. For simplicity, we remove the integer constraint of \( n_{k_1} \) and \( m_{k_2} \). In a network with \( N \) nodes, if service \( k \) can be provided by \( n \) server nodes, \( N - n \) nodes have to access the service via one or more hops in a steady state. For the irregular and asymmetric network, the authors in [32] take a semi-analytical approach in deriving the average hop distance to the servers, \( d, \) as a power-law function of \( n \):

\[
d(n) = A(N/n)^\alpha
\]

Thus, we have

\[
d_{k_1}^A = A(N/n_{k_1})^\alpha, d_{k_2}^B = A(N/m_{k_2})^\alpha
\]

where \( d_{k_1}^A \) and \( d_{k_2}^B \) are the average hop distance to content \( k_1 \)'s copies and computation \( k_2 \)'s dedicated VM copies, respectively.

We assume the average end-to-end latency is proportional to the average hop distance and the scaling factor is \( \eta \). Then the network traffic for duration \( t \) is

\[
T_{total} = \sum_{k_1 \in K_A} T_{k_1}^A + \sum_{k_2 \in K_B} T_{k_2}^B = \eta \left[ \sum_{k_1 \in K_A} \lambda_{k_1}^A \rho_{k_1}^A d_{k_1}^A + \sum_{k_2 \in K_B} \lambda_{k_2}^B \rho_{k_2}^B d_{k_2}^B \right]
\]

According to energy model in Subsection II-E, the total energy consumption for duration \( t \) is as follows:

\[
E_{total} = E_{ca, total} + E_{com, total} = \sum_{k_1 \in K_A} E_{ca,k_1} (n_{k_1}) + E_{tr,k_1} (n_{k_1}) \]

\[
= \sum_{k_2 \in K_B} \left( E_{static} (m_{k_2}) + E_{active} + E_{tr,k_2} (m_{k_2}) \right)
\]

Thus, the caching/computing capacity allocation problem can be formulated as:

\[
\begin{align*}
\min \, E_{total} + \gamma T_{total} \\
s.t. \quad 1 \leq n_{k_1} \leq N \\
1 \leq m_{k_2} \leq N
\end{align*}
\]

We ignore the server capacity constraint by assuming sufficiently large server capacities, since we are more interested in the impact of caching/computing capacity allocation on total network cost than the decision of load balancing among congested servers.

By using the Lagrangian dual method, the optimal \( n_{k_1} \) and \( m_{k_2} \), which are denoted as \( n_{k_1}^* \) and \( m_{k_2}^* \), can be derived as:

\[
\begin{align*}
n_{k_1}^* &= \max[1, \min[n_{k_1}^o, N]] \\
m_{k_2}^* &= \max[1, \min[m_{k_2}^o, N]]
\end{align*}
\]

where \( n_{k_1}^o \) and \( m_{k_2}^o \) are given by

\[
n_{k_1}^o = \left[ A \lambda_k^A \alpha (p_{tr,ink} + p_{tr,node} + \gamma \eta) \right]^{\frac{1}{\alpha + 1}} N^{\frac{1}{\alpha + 1}}
\]

\[
m_{k_2}^o = \left[ A \lambda_k^B \alpha (p_{ca}^t + \gamma \eta) \right]^{\frac{1}{\alpha + 1}} N^{\frac{1}{\alpha + 1}}
\]
\[ m_{k_2}^0 = \left[ \frac{A\lambda_k^A e_k^B \alpha (p_{tr,\text{link}} + p_{tr,\text{node}} + \gamma \eta)}{p_{\text{static}}^B} \right]^{\frac{1}{\gamma \eta}} N^{\frac{1}{\gamma \eta}} \] (21)

\section{The Exhaustive-search Algorithm}

The CCS-SS problem (13) can be denoted by minimizing \( f(H, P|M, R) \) with the caching, computing, link constraints. Note that if the caching/computing strategy matrix \( B \) is pre-known, the formulation (13) will turn into minimizing \( f(P|M, R, H) \) with the link constraints which is a linear optimization problem. In Subsection III-B, we derived the optimal deployment copies \( n_{k_1}^* \) for each content \( k_1 \), and \( m_{k_2}^* \) for computation service \( k_2 \) without regard to copy locations in the network. We assume that the element numbers of \( K_A, K_B \) are \( F_1, F_2 \). Thus, the number of all possible combination subsets of caching/computing strategy (copy locations) \( Q \)

\[ Q = \prod_{k_1 \in K_A} C_{N}^{n_{k_1}} \prod_{k_2 \in K_B} C_{N}^{m_{k_2}} \] (22)

which is significantly reduced in contrast with the original number \( 2^N(F_1 + F_2) \). In the following, we propose an exhaustive-search algorithm to find optimal resource allocation solutions for each service.

We denote the set of all possible combination subsets as

\[ \Phi = \{ H_1, H_2, \ldots, H_Q \} \] (23)

Then, the resource allocation process is described as follows. After the controller selects a caching/computing strategy \( H_q \in \Phi \), it minimizes \( f(P|M, R, H) \) with the link constraints: finding the optimal servers selection \( P \) for the service requests to minimize the combination cost function \( f \). By exhaustive searching, we choose the optimal caching/computing strategy \( H^* \):

\[ H^* = \arg \min_{H_q \in \Phi} f(P|M, R, H_q) \] (24)

and the corresponding \( P^* \) and \( f^* \).

\section{Simulation Results and Discussions}

In this section, we conduct simulations based on a hypothetical United States backbone network US64 [32], which is a representation of the topological characteristics of commercial networks. In the simulation, the parameters of the network are referred to [34]. Energy density of a link is \( p_{tr,\text{link}} = 0.15 \times 10^{-8} \text{J/bit} \). Energy density of a router is in the order of \( p_{tr,\text{node}} = 2 \times 10^{-8} \text{J/bit} \). Power density of caching is \( p_{\text{cach}}^A = 0.25 \times 10^{-8} \text{W/bit} \). Power density of computation VM in the static state is \( p_{\text{static}}^B = 50 \text{W} \). We assume that both content and computation traffic demands are 1Gbps.

\subsection{Network Usage Cost}

In Fig. 2, we show the impact of caching/computing nodes' numbers on the average network traffic per second. We can see that SD-NCC architecture significantly reduces the network traffic compared with the traditional network without in-network caching/computing. This is due to the fact that with in-network caching and computing, large amount of content and computing requests are served on in-network nodes.

\subsection{Optimal Deployment Numbers}

In Subsection III-B, we derive the optimal deployment numbers on minimizing the combination costs of energy consumption and network usage. Fig. 3 shows that under the fixed traffic demand, the optimal deployment number of caching copies for each content is proportional to the service popularity but the optimal deployment number of computation copies for each computation is independent of it. Because the larger number of the same content request (from different users), the less energy on caching (less content need to be cached). In contrast, the energy consumption on computing is fixed. Since computation tasks are more complex and the computation result is difficult to be used for other computation requests, even for the same computation requests from different users.
V. CONCLUSIONS AND FUTURE WORK

In this paper, we proposed to jointly consider networking, caching and computing in a systematic framework to improve the end-to-end system performance. We presented its system model and formulated the joint caching, computing and bandwidth resource allocation problem to minimize the energy cost and network usage cost. In addition, we derived the optimal deployment number of service copies and used an exhaustive-search algorithm to find the near-optimal caching/computing strategy and servers selection. Simulation showed that comparing the traditional network, our proposed SD-NCC framework significantly reduces the traffic traversing the network and has performance advantage on energy consumption. Future work is in progress to consider wireless networks in the proposed framework.

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